# PMGT 501 WBS 5.4 Chapter 7 Exercises 

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Fundamentals of Project Management

PMGT 501

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PMGT 501
Chapter 7: Exercises 1 and 2

1. Given the project information below, what is the probability of completing the National Holiday Toy project in 93 time units?

| Act. ID | Description | Predecessor | Optm. (a) | Most likely (m) | Pess. (b) | Act Time ( $\left.\mathbf{t}_{\mathrm{e}}\right)$ | Variance [(b-a)/6]^2 |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Critical |  |  |  |  |  |  |  |
| 1 | Design package | None | 6 | 12 | 24 |  |  |
| 2 | Design product | 1 | 16 | 19 | 28 |  |  |
| 3 | Build package | 1 | 4 | 7 | 10 |  |  |
| 4 | Secure patent | 2 | 21 | 30 | 39 |  |  |
| 5 | Build product | 2 | 17 | 29 | 47 |  |  |
| 6 | Paint | $3,4,5$ | 4 | 7 | 10 |  |  |
| 7 | Test market | 6 | 13 | 16 | 19 |  |  |

Step 1: Solve for the weighted average activity time $\left(t_{e}\right)$ for each project activity.
Equation 1: $\boldsymbol{t}_{\boldsymbol{e}}=\frac{\boldsymbol{a + 4 m + b}}{\boldsymbol{6}}$ where, $t_{e}=$ weighted average activity time $\mathrm{a}=$ optimistic activity time
$\mathrm{b}=$ pessimistic activity time
$\mathrm{m}=$ most likely activity time

| Act. ID | Description | Predecessor | Optm. (a) | Most likely (m) | Pess. (b) | Act Time ( $\left.\mathbf{t}_{\mathrm{e}}\right)$ | Variance [(b-a)/6]^2 | Critical |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Design package | None | 6 | 12 | 24 | 13 |  |  |
| 2 | Design product | 1 | 16 | 19 | 28 | 20 |  |  |
| 3 | Build package | 1 | 4 | 7 | 10 | 7 |  |  |
| 4 | Secure patent | 2 | 21 | 30 | 39 | 30 |  |  |
| 5 | Build product | 2 | 17 | 29 | 47 | 30 |  |  |
| 6 | Paint | $3,4,5$ | 4 | 7 | 10 | 7 |  |  |
| 7 | Test market | 6 | 13 | 16 | 19 | 16 |  |  |

Step 2: Solve for the activity time variance.
Equation 2: Variance $=\left[\frac{(\boldsymbol{b}-\boldsymbol{a})}{6}\right]^{2}$ where,
$\mathrm{a}=$ optimistic activity time
$\mathrm{b}=$ pessimistic activity time

| Act. ID | Description | Predecessor | Optm. (a) | Most likely (m) | Pess. (b) | Act Time ( $\mathbf{t}_{\mathrm{e}}$ ) | Variance [(b-a)/6]^2 | Critical |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Design package | None | 6 | 12 | 24 | 13 | 9 |  |
| 2 | Design product | 1 | 16 | 19 | 28 | 20 | 4 |  |
| 3 | Build package | 1 | 4 | 7 | 10 | 7 | 1 |  |
| 4 | Secure patent | 2 | 21 | 30 | 39 | 30 | 9 |  |
| 5 | Build product | 2 | 17 | 29 | 47 | 30 | 25 |  |
| 6 | Paint | $3,4,5$ | 4 | 7 | 10 | 7 | 1 |  |
| 7 | Test market | 6 | 13 | 16 | 19 | 16 | 1 |  |

Step 3: Determine which activities are on the critical path.

| Act. ID | Description | Predecessor | Optm. (a) | Most likely (m) | Pess. (b) | Act Time ( $\mathrm{t}_{\mathrm{e}}$ ) | Variance [(b-a)/6]^2 | Critical |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Design package | None | 6 | 12 | 24 | 13 | 9 |  |
| 2 | Design product | 1 | 16 | 19 | 28 | 20 | YES |  |
| 3 | Build package | 1 | 4 | 7 | 10 | 7 | YES |  |
| 4 | Secure patent | 2 | 21 | 30 | 39 | 30 | 1 |  |
| 5 | Build product | 2 | 17 | 29 | 47 | 30 | NO |  |
| 6 | Paint | $3,4,5$ | 4 | 7 | 10 | 7 | 25 | YES |
| 7 | Test market | 6 | 13 | 16 | 19 | 16 | YES |  |



Step 4: Solve for the probability of completing the National Holiday Toy project in 93 time units.
Equation 3: $Z=\frac{T_{S}-T_{E}}{\sqrt{\sum \sigma_{t_{e}}^{2}}}$ where,
$\mathrm{Z}=$ probability of meeting scheduled duration
$T_{E}=$ critical path $=\mathbf{8 6}$ time units
$T_{S}=$ scheduled project duration $=93$ time units
$\sigma_{t_{e}}^{2}=$ variability in the activity time estimates
$Z=\frac{T_{S}-T_{E}}{\sqrt{\sum \sigma_{t_{e}}^{2}}}=\frac{93-86}{\sqrt{49}}=\frac{7}{7}=+1.0$
Answer: $P=.841=84.1 \%$
2. The Global Tea and Organic Juice companies have merged. The following information has been collected for the "Consolidation Project."

1. Compute the expected time for each activity. Expected time for each activity calculated by using formula ( $\boldsymbol{t}_{\boldsymbol{e}}=\frac{\boldsymbol{a + 4 \boldsymbol { m } + \boldsymbol { b }}}{\mathbf{6}}$ ).
2. Compute the variance for each activity. Variance, for each activity was calculated using formula $\left(\right.$ Variance $=\left[\frac{(b-a)}{6}\right]^{2}$ ).

RUNNING HEAD: CHAPT. 7 EXERCISES

| Act. ID | Description | Predecessor | Optm. (a) | Most likely (m) | Pess. (b) | Act Time ( $\mathrm{t}_{\mathrm{e}}$ ) | Variance [(b-a)/6]^2 | Critical |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Codify Accounts | None | 16 | 19 | 28 | 20 | 4 |  |
| 2 | File articles of unification | None | 30 | 30 | 30 | 30 | 0 |  |
| 3 | Unify price and credit policy | None | 60 | 72 | 90 | 73 | 25 |  |
| 4 | Unify personnel policies | None | 18 | 27 | 30 | 26 | 4 |  |
| 5 | Unify data processing | 1 | 17 | 29 | 47 | 30 | 25 |  |
| 6 | Train accounting staff | 1 | 4 | 7 | 10 | 7 | 1 |  |
| 7 | Pilot run data processing | 5 | 12 | 15 | 18 | 15 | 1 |  |
| 8 | Calculate P \& L and balance sheet | 6,7 | 6 | 12 | 24 | 13 | 9 |  |
| 9 | Transfer real property | 2 | 18 | 27 | 30 | 26 | 4 |  |
| 10 | Train salesforce | 3 | 20 | 35 | 50 | 35 | 25 |  |
| 11 | Negotiate with unions | 4 | 40 | 55 | 100 | 60 | 100 |  |
| 12 | Determine capital needs | 8 | 11 | 20 | 29 | 20 | 9 |  |
| 13 | Explain personnel policies | 11 | 14 | 23 | 26 | 22 | 4 |  |
| 14 | Secure line of credit | 9,12 | 13 | 16 | 19 | 16 | 1 |  |
| 15 | End | 10,13,14 | 0 | 0 | 0 | 0 | 0 |  |

3. Compute the expected project duration.

Answer: The expected project duration is $\mathbf{1 1 4}$ time units.

| Act. ID | Description | Predecessor | Optm. (a) | Most likely (m) | Pess. (b) | Act Time ( $\mathrm{t}_{\mathrm{e}}$ ) | Variance [(b-a)/6]^2 | Critical |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Codify Accounts | None | 16 | 19 | 28 | 20 | 4 | YES |
| 2 | File articles of unification | None | 30 | 30 | 30 | 30 | 0 | NO |
| 3 | Unify price and credit policy | None | 60 | 72 | 90 | 73 | 25 | NO |
| 4 | Unify personnel policies | None | 18 | 27 | 30 | 26 | 4 | NO |
| 5 | Unify data processing | 1 | 17 | 29 | 47 | 30 | 25 | YES |
| 6 | Train accounting staff | 1 | 4 | 7 | 10 | 7 | 1 | NO |
| 7 | Pilot run data processing | 5 | 12 | 15 | 18 | 15 | 1 | YES |
| 8 | Calculate P \& L and balance sheet | 6,7 | 6 | 12 | 24 | 13 | 9 | YES |
| 9 | Transfer real property | 2 | 18 | 27 | 30 | 26 | 4 | NO |
| 10 | Train salesforce | 3 | 20 | 35 | 50 | 35 | 25 | NO |
| 11 | Negotiate with unions | 4 | 40 | 55 | 100 | 60 | 100 | NO |
| 12 | Determine capital needs | 8 | 11 | 20 | 29 | 20 | 9 | YES |
| 13 | Explain personnel policies | 11 | 14 | 23 | 26 | 22 | 4 | NO |
| 14 | Secure line of credit | 9,12 | 13 | 16 | 19 | 16 | 1 | YES |
| 15 | End | 10,13,14 | 0 | 0 | 0 | 0 | 0 | YES |

4. What is the probability of completing the project by day $112 ? P=.3897=$ $38.97 \%$. Within 116 days? $P=.6103=61.03 \%$.

- Day 112:

$$
\text { - } Z=\frac{T_{S}-T_{E}}{\sqrt{\sum \sigma_{t_{e}}^{2}}} \text { where, }
$$

- $\mathrm{Z}=$ probability of meeting scheduled duration
- $T_{E}=$ critical path $=114$ time units
- $T_{S}=$ scheduled project duration $=112$ time units
- $\sigma_{t_{e}}^{2}=$ variability in the activity time estimates
- $Z=\frac{T_{S}-T_{E}}{\sqrt{\sum \sigma_{t_{e}}^{2}}}=\frac{\mathbf{1 1 2 - 1 1 4}}{\sqrt{49}}=\frac{-2}{7}=-0.2857$
- Answer: $P=.3897=38.97 \%$
- Day 116:
- $\boldsymbol{Z}=\frac{\boldsymbol{T}_{S}-\boldsymbol{T}_{E}}{\sqrt{\sum \sigma_{t_{e}}^{2}}}$ where,
- $\mathrm{Z}=$ probability of meeting scheduled duration
- $T_{E}=$ critical path $=\mathbf{1 1 4}$ time units
- $T_{S}=$ scheduled project duration $=\mathbf{1 1 6}$ time units
- $\sigma_{t_{e}}^{2}=$ variability in the activity time estimates
- $Z=\frac{T_{S}-T_{E}}{\sqrt{\sum \sigma_{t_{e}}^{2}}}=\frac{\mathbf{1 1 6 - 1 1 4}}{\sqrt{49}}=\frac{2}{7}=0.2857$
- Answer: $P=.6103=61.03 \%$

5. What is the probability of completing "Negotiate with Unions" by day 90 ?

$$
\text { - } Z=\frac{T_{S}-T_{E}}{\sqrt{\sum \sigma_{t_{e}}^{2}}} \text { where, }
$$

- $Z=$ probability of meeting scheduled duration
- $T_{E}=$ critical path $=\mathbf{8 6}$ time units (Comprised of Activity 4 and Activity 11). These are not part of the original critical path, but are the only two items within the path required for the completion of the "Negotiate with Unions" requirement, and are therefore, for consideration of this problem, considered to be the critical path.
- $T_{S}=$ scheduled project duration $=90$ time units
- $\sigma_{t_{e}}^{2}=$ variability in the activity time estimates
- $Z=\frac{T_{S}-T_{E}}{\sqrt{\sum \sigma_{t_{e}}^{2}}}=\frac{90-86}{\sqrt{104}}=\frac{4}{10.198}=0.3922$
- Answer: $P=.6517=65.17 \%$

| Act. ID | Description | Predecessor | Optm. (a) | Most likely (m) | Pess. (b) | Act Time (te) | Variance [(b-a)/6]^2 | Critical |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Codify Accounts | None | 16 | 19 | 28 | 20 | 4 | YES |
| 2 | File articles of unification | None | 30 | 30 | 30 | 30 | 0 |  |
| 3 | Unify price and credit policy | None | 60 | 72 | 90 | 73 | NO |  |
| 4 | Unify personnel policies | None | 18 | 27 | 30 | 26 | 25 | 4 |
| 5 | Unify data processing | 1 | 17 | 29 | 47 | 30 | NO |  |
| 6 | Train accounting staff | 1 | 4 | 7 | 10 | 7 | 25 | NO |
| 7 | Pilot run data processing | 5 | 12 | 15 | 18 | 15 | YES |  |
| 8 | Calculate P \& Land balance sheet | 6,7 | 6 | 12 | 24 | 13 | 1 | 9 |
| 9 | Transfer real property | 2 | 18 | 27 | 30 | 26 | NO |  |
| 10 | Train salesforce | 3 | 20 | 35 | 50 | 35 | 4 | YES |
| 11 | Negotiate with unions | 4 | 40 | 55 | 100 | 60 | 25 | 100 |
| 12 | Determine capital needs | 8 | 11 | 20 | 29 | 20 | NO |  |
| 13 | Explain personnel policies | 11 | 14 | 23 | 26 | 22 | 9 | 4 |
| 14 | Secure line of credit | 9,12 | 13 | 16 | 19 | 16 | NO |  |
| 15 | End | $10,13,14$ | 0 | 0 | 0 | 0 | 1 | 0 |

